

# Package ‘ehymet’

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**Title** Methodologies for Functional Data Based on the Epigraph and Hypograph Indices

**Version** 0.1.0

**Description** Implements methods for functional data analysis based on the epigraph and hypograph indices. These methods transform functional datasets, whether in one or multiple dimensions, into multivariate datasets. The transformation involves applying the epigraph, hypograph, and their modified versions to both the original curves and their first and second derivatives. The calculation of these indices is tailored to the dimensionality of the functional dataset, with special considerations for dependencies between dimensions in multidimensional cases. This approach extends traditional multivariate data analysis techniques to the functional data setting. A key application of this package is the EHyClus method, which enhances clustering analysis for functional data across one or multiple dimensions using the epigraph and hypograph indices.

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**Encoding** UTF-8

**URL** <https://github.com/bpulidob/ehymet>,  
<https://bpulidob.github.io/ehymet/>

**BugReports** <https://github.com/bpulidob/ehymet/issues>

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**Author** Belen Pulido [aut, cre] (<<https://orcid.org/0000-0003-2105-959X>>),  
Jose Ignacio Diez [ctr]

**Maintainer** Belen Pulido <[bpulidob4@gmail.com](mailto:bpulidob4@gmail.com)>

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clustering\_validation *Create a table containing three validation metrics for clustering: Purity, F-measure and Rand Index (RI)*

---

### Description

Create a table containing three validation metrics for clustering: Purity, F-measure and Rand Index (RI)

### Usage

```
clustering_validation(true_labels, clusters)
```

### Arguments

true\_labels Atomic vector with the true labels of the data.  
clusters The clusters predicted by the clustering method.

### Value

A table containing values for Purity, F-measure and RI.

### Examples

```
set.seed(1221)
vars1 <- c("dtaEI", "dtaMEI")
data <- ehymet::sim_model_ex1()
true_labels <- c(rep(1, 50), rep(2, 50))
data_ind <- generate_indices(data)
clus_kmeans <- ehymet::clustInd_kmeans(data_ind, list(vars1))
cluskmeans_mahalanobis_dtaEI dtaMEI <- clus_kmeans$kmeans_mahalanobis_dtaEI dtaMEI$cluster
```

```
clustering_validation(true_labels, clusmeans_mahalanobis_dtaEIIdtaMEI)
```

---

clustInd_hierarch	<i>Perform hierarchical clustering for a different combinations of indices, method and distance</i>
-------------------	---

---

### Description

Perform hierarchical clustering for a different combinations of indices, method and distance

### Usage

```
clustInd_hierarch(
  ind_data,
  vars_combinations,
  method_list = c("single", "complete", "average", "centroid", "ward.D2"),
  dist_vector = c("euclidean", "manhattan"),
  n_cluster = 2,
  true_labels = NULL,
  n_cores = 1
)
```

### Arguments

ind_data	Dataframe containing indices applied to the original data and its first and second derivatives. See <a href="#">generate_indices</a> .
vars_combinations	list containing one or more combinations of indices in ind_data. If it is non-named, the names of the variables are set to vars1, ..., varsk, where k is the number of elements in vars_combinations.
method_list	list of clustering methods.
dist_vector	list of distance metrics.
n_cluster	number of clusters to generate.
true_labels	Vector of true labels for validation (if it is not known true_labels is set to NULL)
n_cores	Number of cores to do parallel computation. 1 by default, which mean no parallel execution.

### Value

A list containing hierarchical clustering results for each configuration.

**Examples**

```
vars1 <- c("dtaEI", "dtaMEI")
vars2 <- c("dtaHI", "dtaMHI")
data <- ehymet::sim_model_ex1()
data_ind <- generate_indices(data)
clustInd_hierarch(data_ind, list(vars1, vars2))
```

---

clustInd\_kkmeans      *Kernel k-means clustering using indices*

---

**Description**

Perform kernel kmeans clustering for a different combinations of indices and kernel

**Usage**

```
clustInd_kkmeans(
  ind_data,
  vars_combinations,
  kernel_list = c("rbfdot", "polydot"),
  n_cluster = 2,
  true_labels = NULL,
  n_cores = 1
)
```

**Arguments**

ind_data	Dataframe containing indices applied to the original data and its first and second derivatives. See <a href="#">generate_indices</a> .
vars_combinations	list containing one or more combinations of indices in ind_data. If it is non-named, the names of the variables are set to vars1, ..., varsk, where k is the number of elements in vars_combinations.
kernel_list	List of kernels
n_cluster	Number of clusters to create
true_labels	Vector of true labels for validation (if it is not known true_labels is set to NULL)
n_cores	Number of cores to do parallel computation. 1 by default, which mean no parallel execution.

**Value**

A list containing kernel-kmeans clustering results for each configuration.

**Examples**

```
vars1 <- c("dtaEI", "dtaMEI")
vars2 <- c("dtaHI", "dtaMHI")
data <- ehymet::sim_model_ex1()
data_ind <- generate_indices(data)
clustInd_kmeans(data_ind, list(vars1, vars2))
```

---

clustInd_kmeans	<i>K-means clustering with indices</i>
-----------------	--

---

**Description**

Perform k-means clustering for a different combinations of indices and distances.

**Usage**

```
clustInd_kmeans(
  ind_data,
  vars_combinations,
  dist_vector = c("euclidean", "mahalanobis"),
  n_cluster = 2,
  true_labels = NULL,
  n_cores = 1
)
```

**Arguments**

ind_data	Dataframe containing indices applied to the original data and its first and second derivatives. See <a href="#">generate_indices</a> .
vars_combinations	list containing one or more combinations of indices in ind_data. If it is non-named, the names of the variables are set to vars1, ..., varsk, where k is the number of elements in vars_combinations.
dist_vector	Atomic vector of distance metrics. The possible values are, "euclidean", "mahalanobis" or both.
n_cluster	Number of clusters to create.
true_labels	Vector of true labels for validation. (if it is not known true_labels is set to NULL)
n_cores	Number of cores to do parallel computation. 1 by default, which mean no parallel execution.

**Value**

A list containing hierarchical clustering results for each configuration

A list containing kmeans clustering results for each configuration

**Examples**

```
vars1 <- c("dtaEI", "dtaMEI")
vars2 <- c("dtaHI", "dtaMHI")
data <- ehymet::sim_model_ex1()
data_ind <- generate_indices(data)
clustInd_kmeans(data_ind, list(vars1, vars2))
```

---

clustInd\_spc

*Spectral clustering using indices*


---

**Description**

Perform spectral clustering for a different combinations of indices and kernels

**Usage**

```
clustInd_spc(
  ind_data,
  vars_combinations,
  kernel_list = c("rbfdot", "polydot"),
  n_cluster = 2,
  true_labels = NULL,
  n_cores = 1
)
```

**Arguments**

ind_data	Dataframe containing indices applied to the original data and its first and second derivatives. See <a href="#">generate_indices</a> .
vars_combinations	list containing one or more combinations of indices in ind_data. If it is non-named, the names of the variables are set to vars1, ..., varsk, where k is the number of elements in vars_combinations.
kernel_list	List of kernels
n_cluster	Number of clusters to create
true_labels	Vector of true labels for validation (if it is not known true_labels is set to NULL)
n_cores	Number of cores to do parallel computation. 1 by default, which mean no parallel execution.

**Value**

A list containing kmeans clustering results for each configuration

**Examples**

```
vars1 <- c("dtaEI", "dtaMEI")
vars2 <- c("dtaHI", "dtaMHI")
data <- ehymet::sim_model_ex1()
data_ind <- generate_indices(data)
clustInd_spc(data_ind, list(vars1, vars2))
```

EHyClus

*Clustering using Epigraph and Hypograph indices***Description**

It creates a multivariate dataset containing the epigraph, hypograph and/or its modified versions on the curves and derivatives and then perform hierarchical clustering, kmeans, kernel kmeans, and spectral clustering

**Usage**

```
EHyClus(
  curves,
  vars_combinations,
  k = 30,
  n_clusters = 2,
  bs = "cr",
  clustering_methods = c("hierarch", "kmeans", "kkmeans", "spc"),
  l_method_hierarch = c("single", "complete", "average", "centroid", "ward.D2"),
  l_dist_hierarch = c("euclidean", "manhattan"),
  l_dist_kmeans = c("euclidean", "mahalanobis"),
  l_kernel = c("rbfdot", "polydot"),
  grid,
  true_labels = NULL,
  only_best = FALSE,
  verbose = FALSE,
  n_cores = 1
)
```

**Arguments**

**curves** Dataset containing the curves to apply a clustering algorithm. The functional dataset can be one dimensional ( $n \times p$ ) where  $n$  is the number of curves and  $p$  the number of time points, or multidimensional ( $n \times p \times q$ ) where  $q$  represents the number of dimensions in the data

**vars\_combinations** If list, each element of the list should be an atomic vector of strings with the names of the variables. Combinations with non-valid variable names will be discarded. If the list is non-named, the names of the variables are set to vars1,

..., varsk, where k is the number of elements in vars\_combinations. If not provided, generic combinations of variables will be used. They will not be the same for uni-dimensional and multi-dimensional problems.

k	Number of basis functions for the B-splines. If equals to 0, the number of basis functions will be automatically selected.
n_clusters	Number of clusters to generate.
bs	A two letter character string indicating the (penalized) smoothing basis to use. See <a href="#">smooth.terms</a> .
clustering_methods	character vector specifying at least one of the following clustering methods to be computed: "hierarch", "kmeans", "kkmeans" or "spc".
l_method_hierarch	list of clustering methods for hierarchical clustering.
l_dist_hierarch	list of distances for hierarchical clustering.
l_dist_kmeans	list of distances for kmeans clustering.
l_kernel	list of kernels for kkmeans or spc.
grid	Atomic vector of type numeric with two elements: the lower limit and the upper limit of the evaluation grid. If not provided, it will be selected automatically.
true_labels	Numeric vector of true labels for validation. If provided, evaluation metrics are computed in the final result.
only_best	logical value. If TRUE and true_labels is provided, the function will return only the result for the best clustering method based on the Rand Index. Defaults to FALSE.
verbose	If TRUE, the function will print logs for about the execution of some clustering methods. Defaults to FALSE.
n_cores	Number of cores to do parallel computation. 1 by default, which mean no parallel execution. Must be an integer number greater than 1.

### Value

A list containing the clustering partition for each method and indices combination and, if true\_labels is provided a data frame containing the time elapsed for obtaining a clustering partition of the indices dataset for each methodology. Also, the number of generated clusters and the combinations of variables used can be seen as attributes of this object.

### Examples

```
# univarariate data without labels
curves <- sim_model_ex1(n = 10)
vars_combinations <- list(c("dtaEI", "dtaMEI"), c("dtaHI", "dtaMHI"))
EHyClus(curves, vars_combinations = vars_combinations)

# multivariate data with labels
curves <- sim_model_ex2(n = 5)
true_labels <- c(rep(1, 5), rep(2, 5))
```



```

vars_combinations <- list(c("dtaMEI", "ddtaMEI"), c("dtaMEI", "d2dtaMEI"))
res <- EHyClus(curves, vars_combinations = vars_combinations, true_labels = true_labels)
res$cluster # clustering results

# multivariate data and generic (default) vars_combinations
curves <- sim_model_ex2(n = 5)
EHyClus(curves)

```

---

EI

*Epigraph Index (EI) for a functional dataset*


---

### Description

The Epigraph Index of a curve  $x$  is one minus the proportion of curves in the sample that are above  $x$ .

### Usage

```
EI(curves, ...)
```

### Arguments

curves	matrix where each row represents a curve, and each column represents values along the curve or array with dimension $n \times p \times q$ with $n$ curves, $p$ values along the curve, and $q$ dimensions.
...	Ignored.

### Value

numeric vector containing the EI for each curve.

### Examples

```

x <- matrix(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7), ncol = 3, nrow = 4)
EI(x)

y <- array(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7, -1, -5, -6, 2, 3, 0, -1, 0, 2, -1, -2, 0),
  dim = c(3, 4, 2)
)
EI(y)

```

---

generate_indices	<i>Create a dataset with indices from a functional dataset in one or multiple dimensions</i>
------------------	--

---

### Description

Create a dataset with indices from a functional dataset in one or multiple dimensions

### Usage

```
generate_indices(
  curves,
  k,
  grid,
  bs = "cr",
  indices = c("EI", "HI", "MEI", "MHI"),
  ...
)
```

### Arguments

curves	matrix with dimension $n \times p$ in the case of a one-dimensional functional dataset, or array of dimension $n \times p \times q$ in the case of a multivariate functional dataset. $n$ represents the number of curves, $p$ the number of values along the curve, and in the second case, $q$ is the number of dimensions.
k	Number of basis functions for the B-splines. If equals to 0, the number of basis functions will be automatically selected.
grid	Atomic vector of type numeric with two elements: the lower limit and the upper limit of the evaluation grid. If not provided, it will be selected automatically.
bs	A two letter character string indicating the (penalized) smoothing basis to use. See <a href="#">smooth.terms</a> .
indices	Set of indices to be applied to the dataset. They should be any between EI, HI, MEI and MHI.
...	Additional arguments (unused)

### Value

A dataframe containing the indices provided in indices for original data, first and second derivatives

### Examples

```
x1 <- array(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7, -1, -5, -6, 2, 3, 0, -1, 0, 2, -1, -2, 0),
  dim = c(3, 4, 2)
)
generate_indices(x1, k = 4)
```

```
x2 <- matrix(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7), nrow = 3, ncol = 4)
generate_indices(x2, k = 4)
```

---

HI *Hypograph Index (HI) for a functional dataset*

---

### Description

The Hypograph Index of a curve  $x$  is the proportion of curves in the sample that are below  $x$ .

### Usage

```
HI( curves, ... )
```

### Arguments

curves	matrix where each row represents a curve, and each column represents values along the curve or array with dimension $n \times p \times q$ with $n$ curves, $p$ values along the curve, and $q$ dimensions.
...	Ignored.

### Value

numeric vector containing the HI for each curve.

### Examples

```
x <- matrix(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7), ncol = 3, nrow = 4)
HI(x)

y <- array(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7, -1, -5, -6, 2, 3, 0, -1, 0, 2, -1, -2, 0),
  dim = c(3, 4, 2)
)
HI(y)
```

---

 MEI

*Modified Epigraph Index (MEI) for functional dataset.*


---

**Description**

The Modified Epigraph Index of a curve  $x$  is one minus the proportion of "time" the curves in the sample are above  $x$ .

**Usage**

```
MEI(curves, ...)
```

**Arguments**

curves	matrix where each row represents a curve, and each column represents values along the curve or an array with dimension $n \times p \times q$ with $n$ curves, $p$ values along the curve, and $q$ dimensions.
...	Ignored.

**Value**

numeric vector containing the MEI for each curve.

**Examples**

```
x <- matrix(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7), ncol = 3, nrow = 4)
MEI(x)
y <- array(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7, -1, -5, -6, 2, 3, 0, -1, 0, 2, -1, -2, 0),
  dim = c(3, 4, 2)
)
MEI(y)
```

---

 MHI

*Modified Hypograph Index (MHI) for a functional dataset*


---

**Description**

The Modified Hypograph Index of a curve  $x$  is the proportion of "time" the curves in the sample are below  $x$ .

**Usage**

```
MHI(curves, ...)
```

**Arguments**

curves matrix where each row represents a curve, and each column represents values along the curve or an array with dimension  $n \times p \times q$  with  $n$  curves,  $p$  values along the curve, and  $q$  dimensions.

... Ignored.

**Value**

numeric vector containing the MHI for each curve.

**Examples**

```
x <- matrix(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7), ncol = 3, nrow = 4)
MHI(x)
y <- array(c(1, 2, 3, 3, 2, 1, 5, 2, 3, 9, 8, 7, -1, -5, -6, 2, 3, 0, -1, 0, 2, -1, -2, 0),
  dim = c(3, 4, 2)
)
MHI(y)
```

---

sim\_model\_ex1

*Function for generating functional data in one dimension*


---

**Description**

Each dataset has 2 groups with  $n$  curves each, defined in the interval  $t = [0, 1]$  with  $p$  equidistant points. The first  $n$  curves are generated from the following model  $X_1(t) = E_1(t) + e(t)$  where  $E_1(t) = E_1(X(t)) = 30t^{\frac{3}{2}}(1-t)$  is the mean function and  $e(t)$  is a centered Gaussian process with covariance matrix  $Cov(e(t_i), e(t_j)) = 0.3 \exp(-\frac{|t_i - t_j|}{0.3})$ . The remaining 50 functions are generated from model `i_sim` with `i_sim`  $\in \{1, \dots, 8\}$ . The first three models contain changes in the mean, while the covariance matrix does not change. Model 4 and 5 are obtained by multiplying the covariance matrix by a constant. Model 6 is obtained from adding to  $E_1(t)$  a centered Gaussian process  $h(t)$  whose covariance matrix is given by  $Cov(e(t_i), e(t_j)) = 0.5 \exp(-\frac{|t_i - t_j|}{0.2})$ . Model 7 and 8 are obtained by a different mean function.

**Model 1.**  $X_1(t) = 30t^{\frac{3}{2}}(1-t) + 0.5 + e(t)$ .

**Model 2.**  $X_2(t) = 30t^{\frac{3}{2}}(1-t) + 0.75 + e(t)$ .

**Model 3.**  $X_3(t) = 30t^{\frac{3}{2}}(1-t) + 1 + e(t)$ .

**Model 4.**  $X_4(t) = 30t^{\frac{3}{2}}(1-t) + 2e(t)$ .

**Model 5.**  $X_5(t) = 30t^{\frac{3}{2}}(1-t) + 0.25e(t)$ .

**Model 6.**  $X_6(t) = 30t^{\frac{3}{2}}(1-t) + h(t)$ .

**Model 7.**  $X_7(t) = 30t(1-t)^2 + h(t)$ .

**Model 8.**  $X_8(t) = 30t(1-t)^2 + e(t)$ .

**Usage**

```
sim_model_ex1(n = 50, p = 30, i_sim = 1)
```

**Arguments**

n	Number of curves to generate for each of the two groups. Set to 50 by default.
p	Number of grid points of the curves. Curves are generated over the interval $[0, 1]$ . Set to 30 grid point by default.
i_sim	Integer set to $1, \dots, 8$ .

**Value**

data matrix of size  $2n \times p$ .

**Examples**

```
sm1 <- sim_model_ex1()
dim(sm1)
```

---

sim\_model\_ex2

*Function for generating functional data in one or multiple dimension*

---

**Description**

The function can generate one-dimensional or multi-dimensional curves. For `i_sim` 1 or 2, one-dimensional curves are generated. For `i_sim` 3 or 4, multi-dimensional curves are generated. ADD REFERENCES

**Usage**

```
sim_model_ex2(n = 50, p = 150, i_sim = 1)
```

**Arguments**

n	Number of curves to generate for each of the two groups. Set to 50 by default.
p	Number of grid points of the curves. Curves are generated over the interval $[0, 1]$ . Set to 150 grid point by default.
i_sim	Integer set to $1, \dots, 4$ NULL by default in which case a seed is not set.

**Value**

data matrix of size  $2n \times p$  if `i_sim`  $\in 1, 2$  or an array of dimensions  $2n \times p \times 2$  if `i_sim`  $\in 3, 4$ .

**Examples**

```
sm1 <- sim_model_ex2()
dim(sm1) # This should output (100, 150) by default, since n = 50 and p = 150

sm4 <- sim_model_ex2(i_sim = 4)
dim(sm4) # This should output (100, 150, 2) by default, since n = 50 and p = 150
```

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