

$$\begin{aligned} A &= \lim_{n \rightarrow \infty} \Delta x \left( a^2 + \left( a^2 + 2a\Delta x + (\Delta x)^2 \right) \right. \\ &+ \left( a^2 + 2 \cdot 2a\Delta x + 2^2 (\Delta x)^2 \right) + \left( a^2 + 2 \cdot 3a\Delta x + 3^2 (\Delta x)^2 \right) \\ &\quad + \dots \\ &\quad \left. + \left( a^2 + 2 \cdot (n-1)a\Delta x + (n-1)^2 (\Delta x)^2 \right) \right) \\ &= \frac{1}{3} (b^3 - a^3) \end{aligned}$$